

# AN INTRODUCTION TO MICROFLUIDICS :

## Lecture n°4

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## Outline of Lecture 1

- 1 - History and prospectives of microfluidics
- 2 - Microsystems and macroscopic approach.
- 3 - The spectacular changes of the balances of forces as we go to the small world.

## Outline of Lecture 2

- The fluid mechanics of microfluidics
- Digital microfluidics

## Outline of Lecture 3

- 1 - Basic notions on diffusive processes
- 2 - Micromixing
- 3 - Microreactors.

## Outline of Lecture 4

- 1 - Electroosmosis, electrophoresis
- 2 - Miniaturisation of separation systems
- 3 - An example of a lab on a chip

Electrophoresis : Charged particles migrate

Electroosmose : Fluid is driven by charged layers close to the walls

Diélectrophoresis : Particles move under the effect a gradient of Electric field.

Using electric fields in miniaturized systems is easy because

$$E \sim V/l$$

# A FEW THINGS TO KNOW ABOUT ELECTROKINETICS

## 1 - Electrophoresis

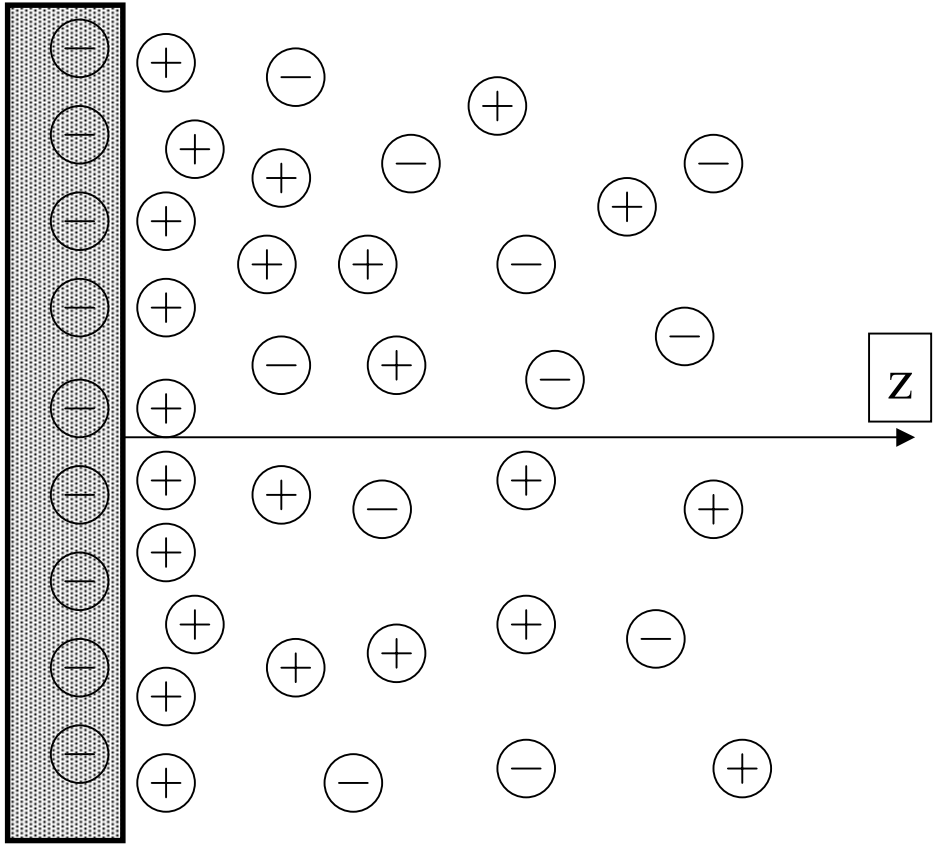
Coulomb law  $F = qE$

In a fluid, the flow equations are

$$qE - F_v = m \frac{dV}{dt} \approx 0 \quad F_v = 6\pi R\mu V$$

$$V = \mu_e E \quad \text{with} \quad \mu_e = \frac{q}{6\pi R\mu}$$

# Double electric layer



$\rho_e$

# CHARACTERISTICS OF THE DEBYE HUCKEL LAYER

Electrical Potential

$$\psi = \zeta e^{-z / \lambda_D}$$

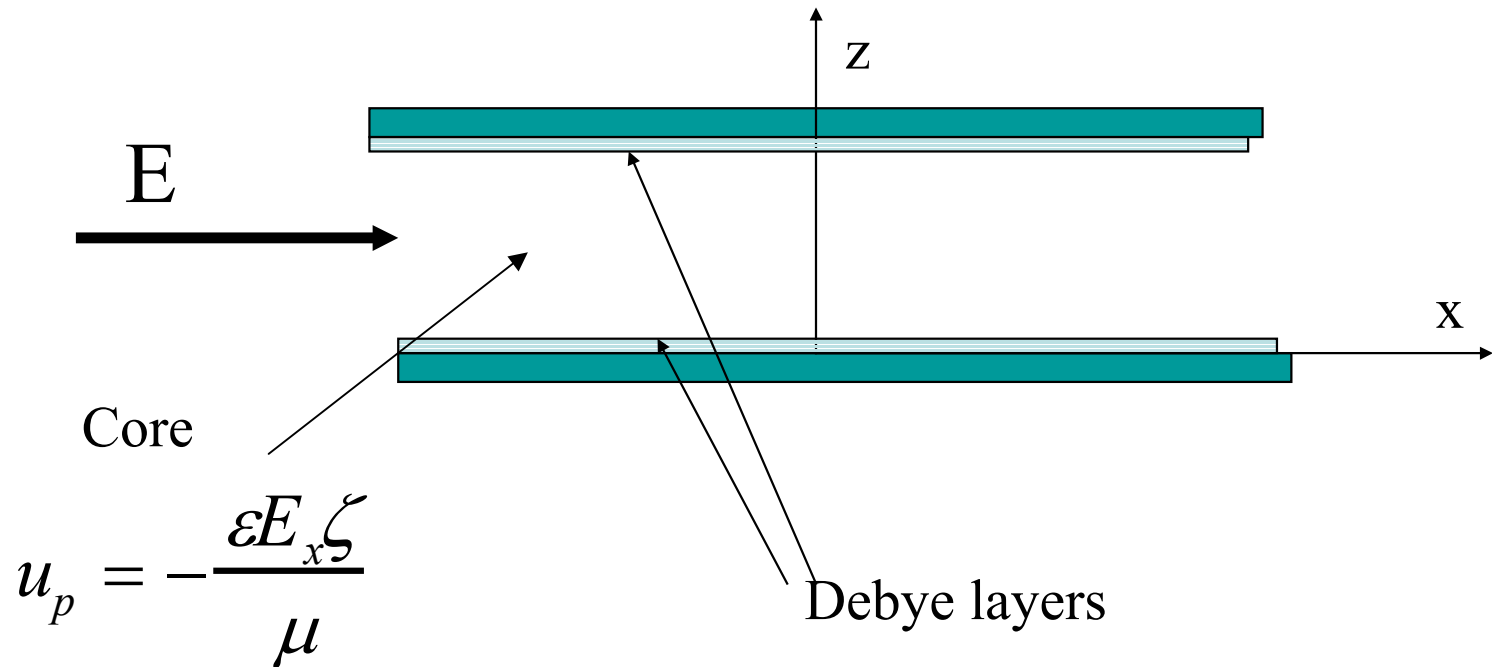
Thickness

$$\lambda_D = \sqrt{\frac{D \varepsilon}{\sigma}}$$

*Debye-Huckel length*

# ELECTROOSMOSIS

3) Electroosmosis = Flow of an electrolyte produced by the presence of an electric field driving the charged layer close to the walls



$$u_p = -\frac{\epsilon E_x \zeta}{\mu}$$



Vitesse de Smoluchowsky

# STREAMING POTENTIAL

The inverse effect of electroosmosis

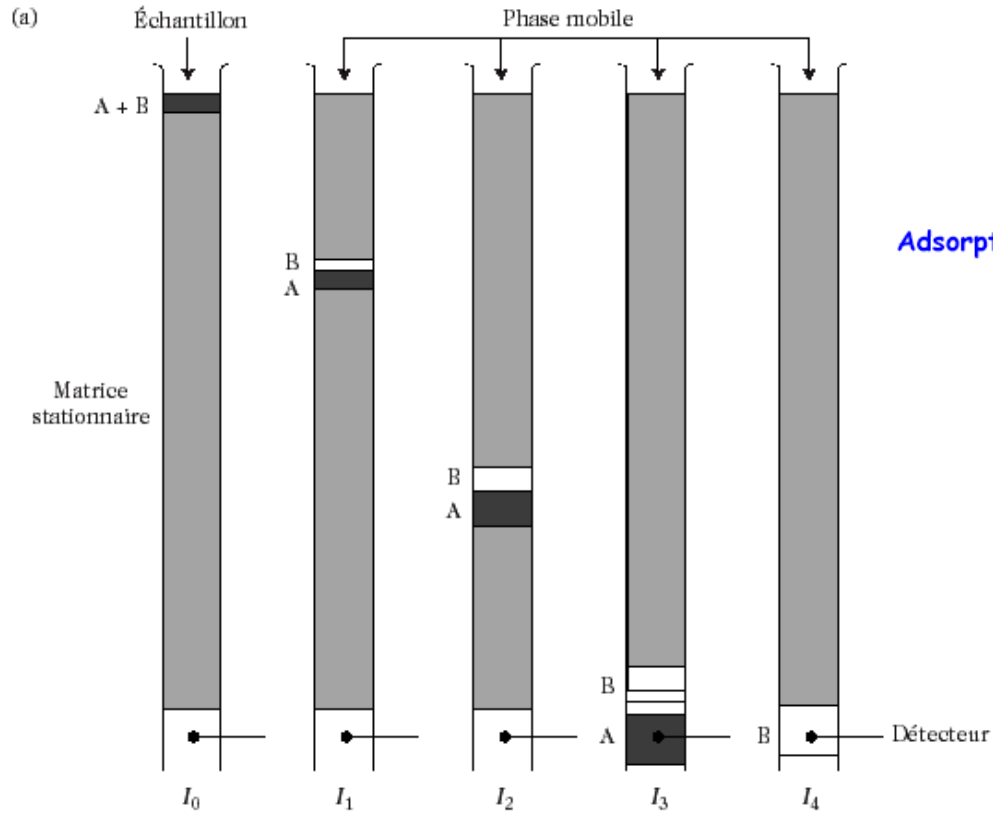


A flow generates an electric field

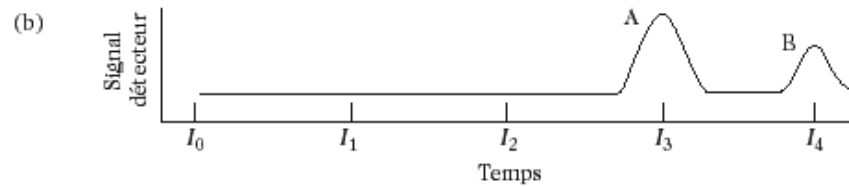
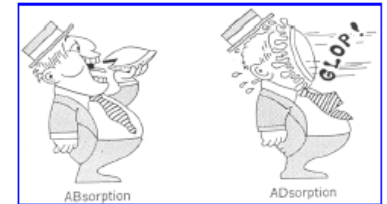
## Various fields requiring separation sciences

- Pharmaceutical and other various industries
- Public health
- Food security (involves environment, agriculture, fishing, food production industry, packaging...)
- Environmental protection
- Safety of manufactured products (ex: toys for infants)
- Frauds and counterfeiting
- Doping
- Historical heritage, archeology

# Principle of chromatography

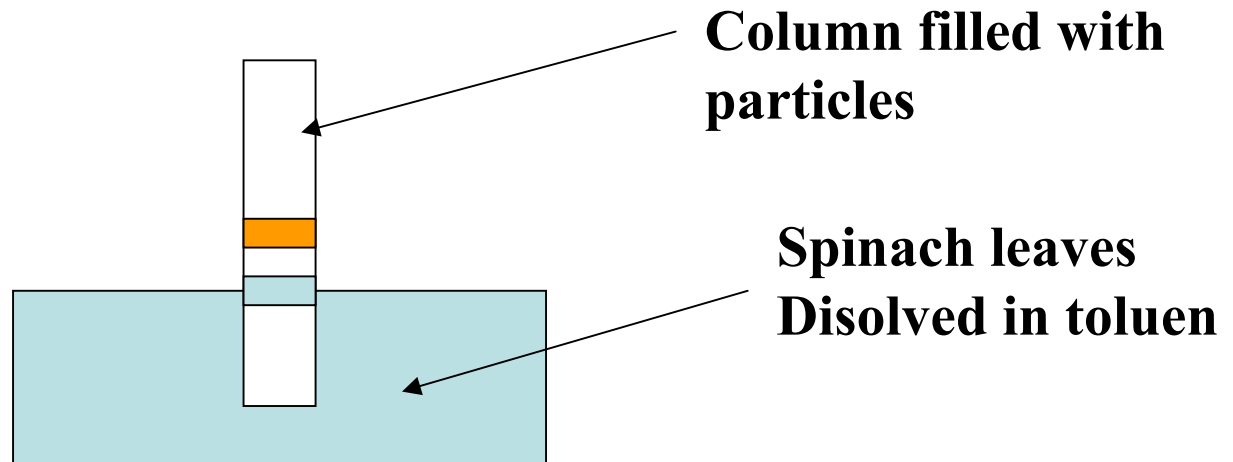


Adsorption chromatography

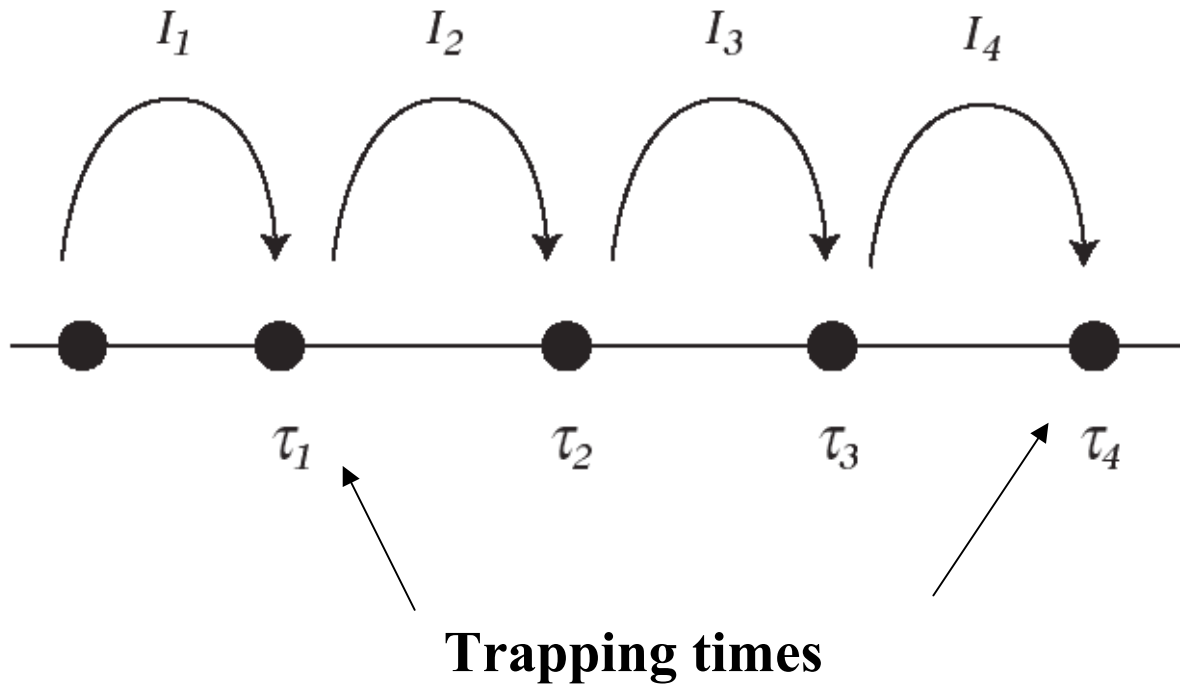


# Microfluidics and separation techniques

The first separation experiment was done by Tswett (1902)  
This led to the discovery of chlorophyll.



# Statistical model for chromatography



# 5 fundamental types of chromatography



Adsorption



Affinité

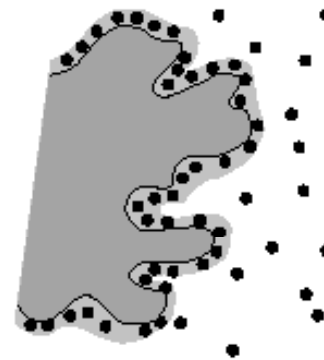


Échange d'ions

(a)



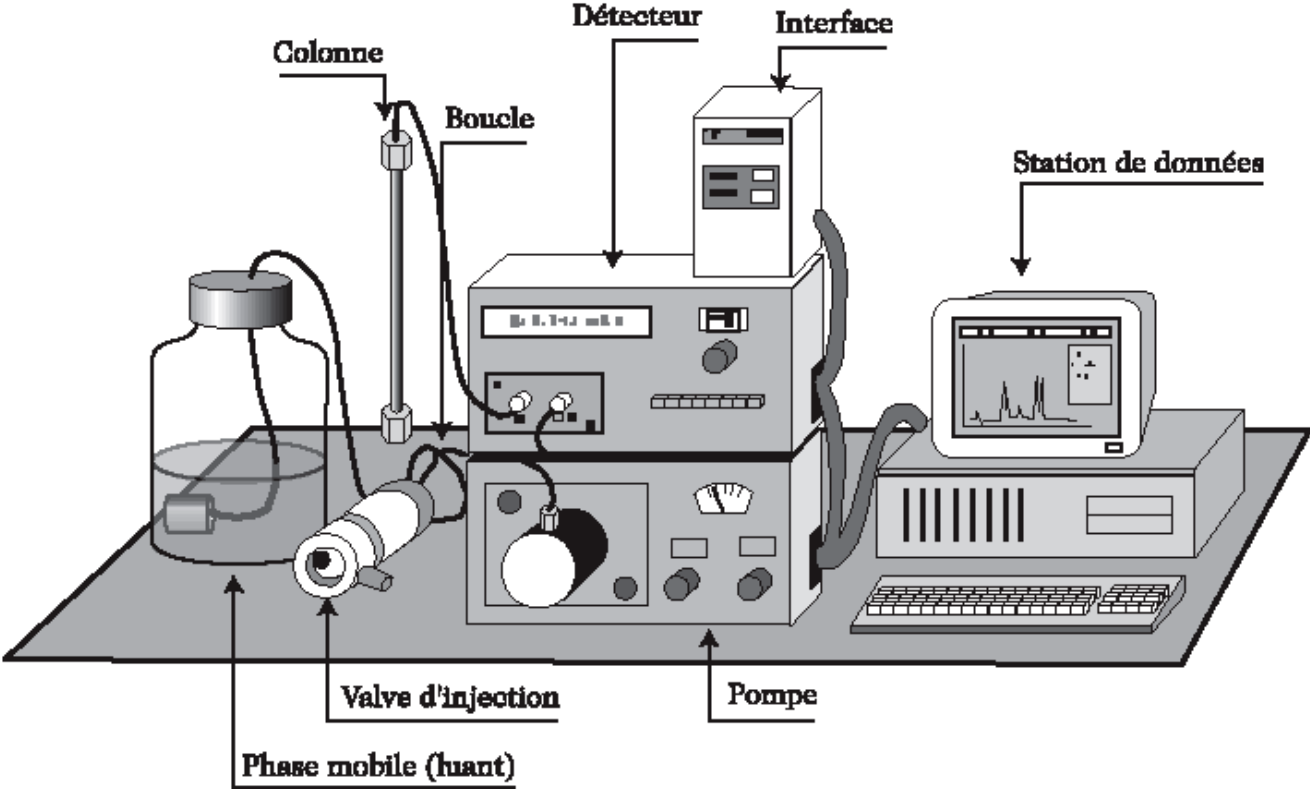
Exclusion



Partition

(b)

# A typical equipment for HPLC



# Electrophoretic separation

For an isolated particle of charge  $q$ , mass  $m$ , Coulomb force reads :

$$F = qE$$

In a fluid, the charged particle move according to the law :

$$qE - F_v = m \frac{dV}{dt} \approx 0 \quad F_v = 6\pi R \mu V$$

Therefore

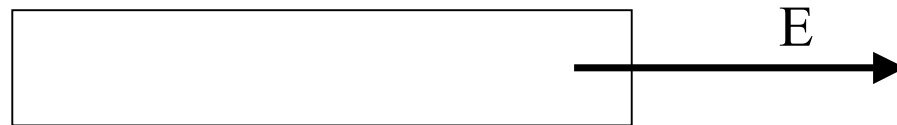
Viscous friction

$$V = \mu_e E \quad \text{where} \quad \mu_e = \frac{q}{6\pi R \eta}$$

**Separation is feasible, because ions with different ratio  $q/R$  will migrate at different speeds**

# Separation techniques using electric fields

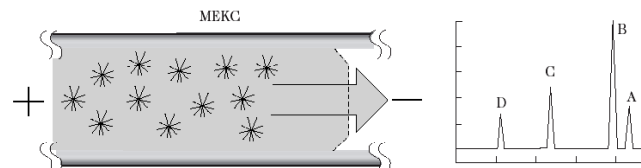
- FSCE : Electrophoresis in a free medium



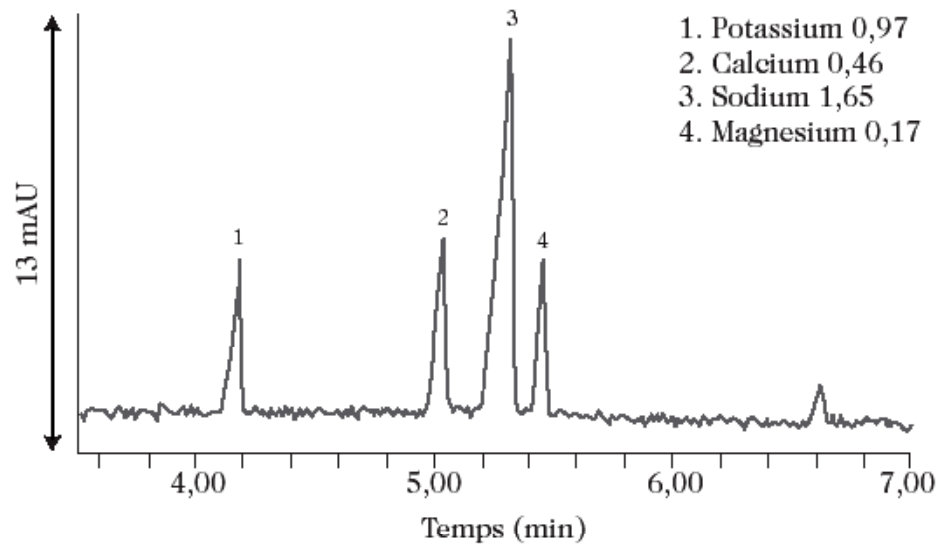
- CEC : Capillary Electro Chromatography (a gel is used)



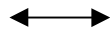
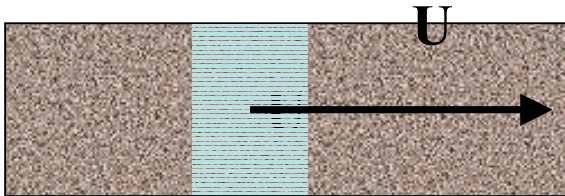
- MEKC : Micellar ElectroKinetic chromatography



## Un exemple de un électrochromatogramme



## How much the bands spread ?



$$\delta = \sqrt{D_{\text{eff}} t}$$

**Taylor  
Aris estimate**

$$D_{\text{eff}} = Pe^2 D_i + U^2 b^2 / D$$

SOME IMPORTANT QUANTITIES USEFUL FOR THE  
CHARACTERIZATION OF THE PERFORMANCES  
OF THE SEPARATION TECHNIQUE

# The number of theoretical plates

$$N = \left( \frac{\text{distance parcourue par la bande}}{\text{largeur diffusive de la bande}} \right)^2$$

$$N \sim \frac{L^2}{D_{eff}(L/U)} \sim \frac{UL}{D_{eff}}$$

**Basic data: column number plates**

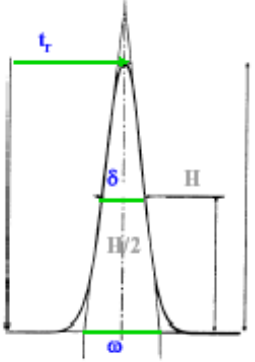
- Separations based on the distribution of the analyte A between the stationary phase S and the mobile phase M

$$K = \frac{C_s}{C_m}$$

- If the injected amount is low  
→ Gaussian peak

$$N = \left( \frac{t_R}{\sigma} \right)^2 = 5,54 \left( \frac{t_R}{\delta} \right)^2 = 16 \left( \frac{t_R}{\omega} \right)^2$$

N column number plates ;  $\sigma^2$  peak variance  
( $\sigma$  standard deviation)



Merle-Claire Hennion, Laboratoire Environnement et Chimie Analytique, ESPCI

(From M.C.Hennion (2004))

**One infers**

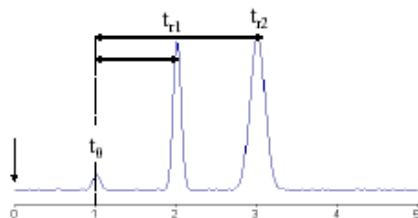
Retention time in the  
column

$$N \sim \frac{UL}{D_{eff}} \sim \frac{ULD}{U^2 b^2} \sim \frac{LD}{Ub^2} \sim \frac{t_R D}{b^2}$$

**Number of theoretical plates**

# OTHER QUANTITIES OF INTEREST

## Selectivity



$$\alpha = \frac{t_2 - t_0}{t_1 - t_0} = \frac{k_2'}{k_1'} = \frac{K_2}{K_1}$$

$\alpha$  sélectivité

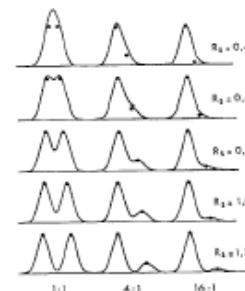
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## Resolution (1)

$$R = \frac{2(t_{R2} - t_{R1})}{\omega_2 + \omega_1}$$

• si  $\omega_2 \approx \omega_1 \Rightarrow R \approx \frac{1}{4} \left( \frac{\alpha - 1}{\alpha} \right) \left( \frac{k_2}{1 + k_2} \right) \sqrt{N_2}$   
(Purnell relation)

• si  $N_2 \approx N_1 \Rightarrow R \approx \frac{1}{2} \left( \frac{\alpha - 1}{\alpha + 1} \right) \left( \frac{\bar{k}}{1 + \bar{k}} \right) \sqrt{N}$   
(Said relation)



— Allure des chromatogrammes en fonction de la résolution  $R_2$  (de 0,4 à 1,25) et des surfaces relatives des deux pics. Les points indiquent les sommets des pics pour chaque soluté (courbes calculées)

Marie-Claire Hennion, Laboratoire Environnement et Chimie Analytique, ESPCI

(From M.C.Hennion (2004))

# *IS MINIATURIZATION ADVANTAGEOUS ?*

## 1) NON ELECTRICAL SEPARATION TECHNIQUES

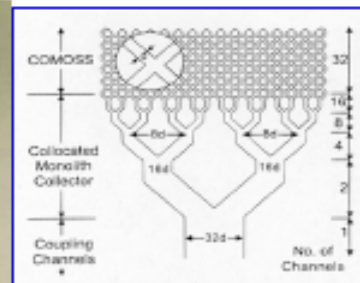
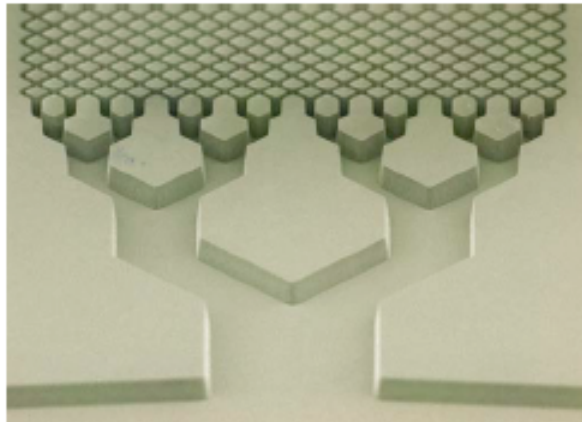
- Small samples
- Intégration possible
- Parallelism possible

**But no improvement of the analytical performances**

$$N \sim \frac{t_R D}{b^2} \sim l^0 \qquad t_R \sim l/U \sim l^0$$

## Nanocolumns for chromatography

COMOSS = "collocated monolith support structure"



*Structure quartz, plots 5x5  $\mu\text{m}$   
profondeur 10  $\mu\text{m}$ , séparés par  
microcanaux de 1,5  $\mu\text{m}$*

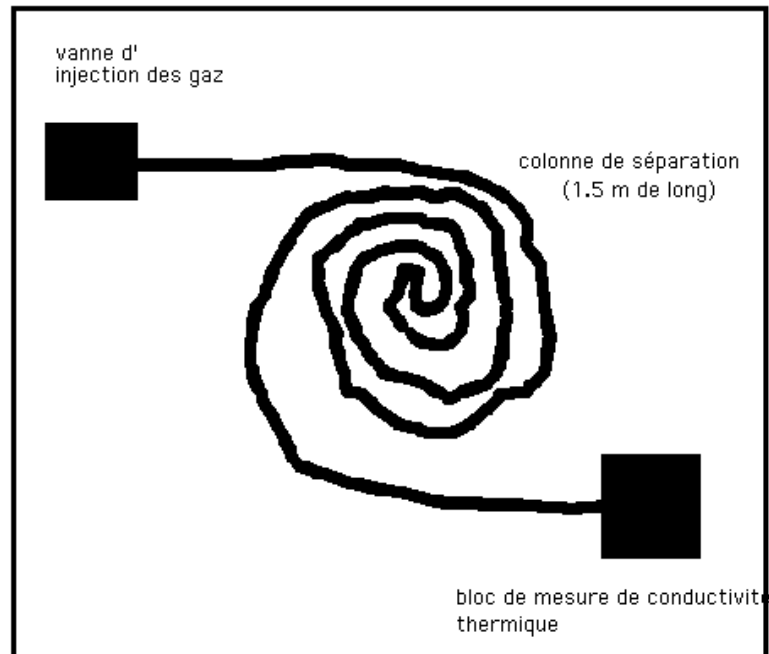
*Volume = 18 nL (COMOSS de 4,5  
cm long par 150  $\mu\text{m}$ ), surface 480  
 $\mu\text{m}^2$*

*(D'après F. Regnier et al., Anal. Chem., 70(1998)3790)*

*Merle-Cibire Hennion, Laboratoire Environnement et Chimie Analytique, ESPCI*

(From M.C.Hennion (2004))

# Le premier lab on a chip était une colonne chromatographique à gaz (Terry, 1975)



## 2)Electrical separation techniques

$$N \sim \frac{\mu_{EOF} EL}{D}$$

Number of theoretical plates

Maximum electrical field that can be applied

$$Q \sim K \Delta T l \sim K \sigma E^2 l^3$$

Therefore

$$E \sim l^{-1}$$

Thereby

$$N \sim l^0$$

**The number of plates remains the same, while the retention time becomes :**

$$t_R \sim L/V \sim l^2$$

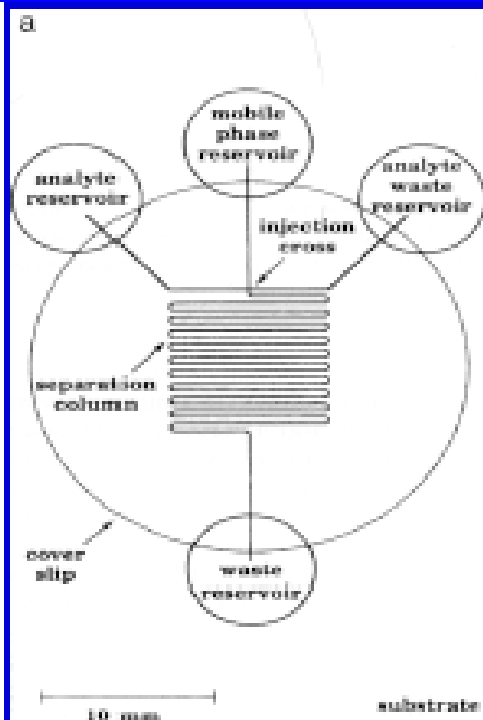
**Conclusion : it is tremendously advantageous**

- Same performances, must smaller times
- (800  $\mu$ s, Jacobson et al)

Miniaturization in this case thus leads to :

- Small volumes
- Intégration and parallélization possible
- Conservation of the efficiency of the column
- Considerable gain of time

## The first chip electrochromatography



- Glass structure
- 5 cm × 2,5 cm (serpentine 1 cm × 1 cm)
- Channel : 165 mm long, 10- $\mu$ m deep, 90- $\mu$ m wide at surface, 70  $\mu$ m at the bottom
- Peak broadening due to the U-turns
- Reproducibility of injection ( $\approx$ 90 pL in pinched mode and  $\approx$  300 pL en gating mode)

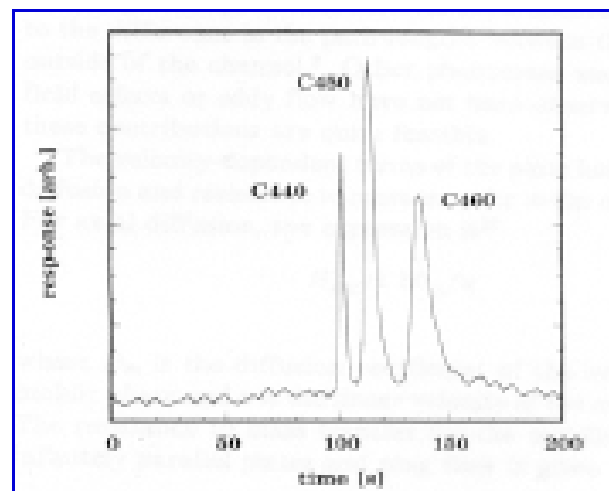
*(D'après M. Ramsey, Anal. Chem. 66(1994)1107)*

*Marie-Claire Hennion, Laboratoire Environnement et Chimie Analytique, ESPCI*

(From M.C.Hennion (2004))

## The first chip electrochromatography

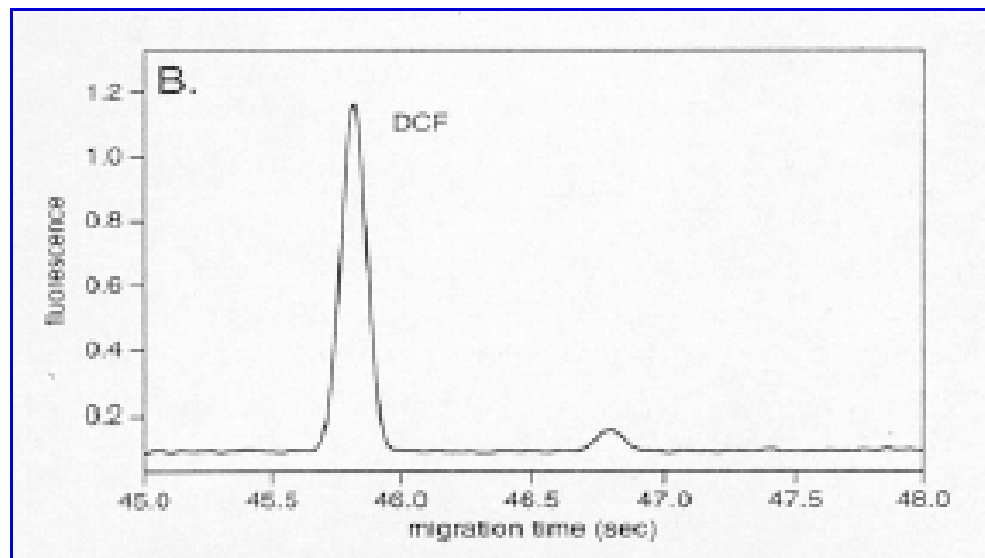
- ❑ In situ bonding of the canal surface with octadecylsilane
- ❑ Electroosmotic flow for both injection and separation
- ❑ Plate number : 11700 for C440, 2950 for C450 and 1290 for C460
- ❑ Peak broadening due to the serpentine shape



*Separation of 3 coumarines, tetraborate buffer, pH 9,2, 10mM with 25% acétonitrile,  $u=0,65$  mm/s ( $V=138V/cm$ )*

*(S. Jacobson et al, Anal.Chem., 66(1994)2369)*

More than 1 million plates within 46 seconds

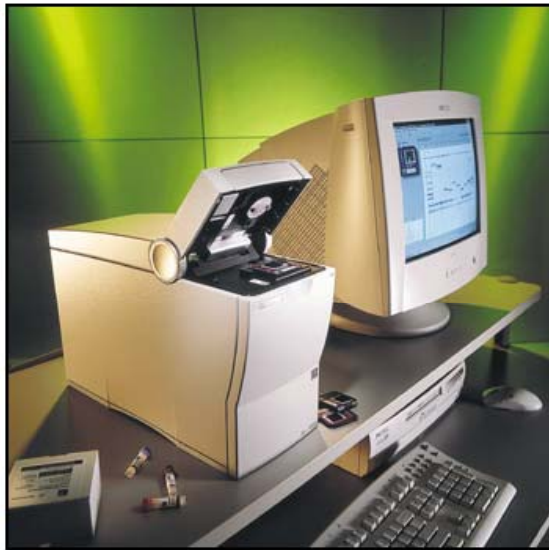


*Electrophoregramme of dichlorofluoresceine and impurity*  
*1170 V/cm, 22,2 cm spiral, boric acid 20mM with TRIS buffer 100mM*  
**N= 1 100 000 plateaux**

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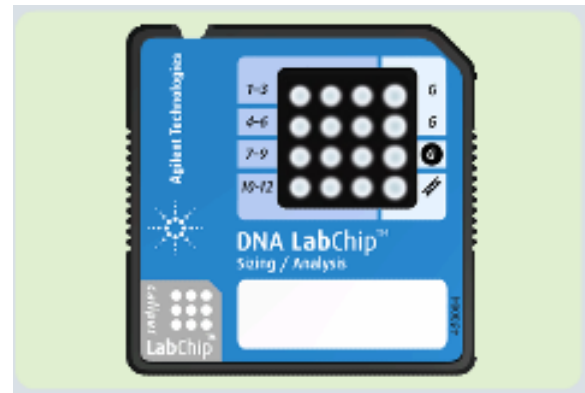
(From M.C.Hennion (2004))

# A microfluidic system for DNA separation



**From Agilent-  
Caliper**

**Allow to characterize DNA  
Fragments with excellent  
Resolution, and in a small  
time**



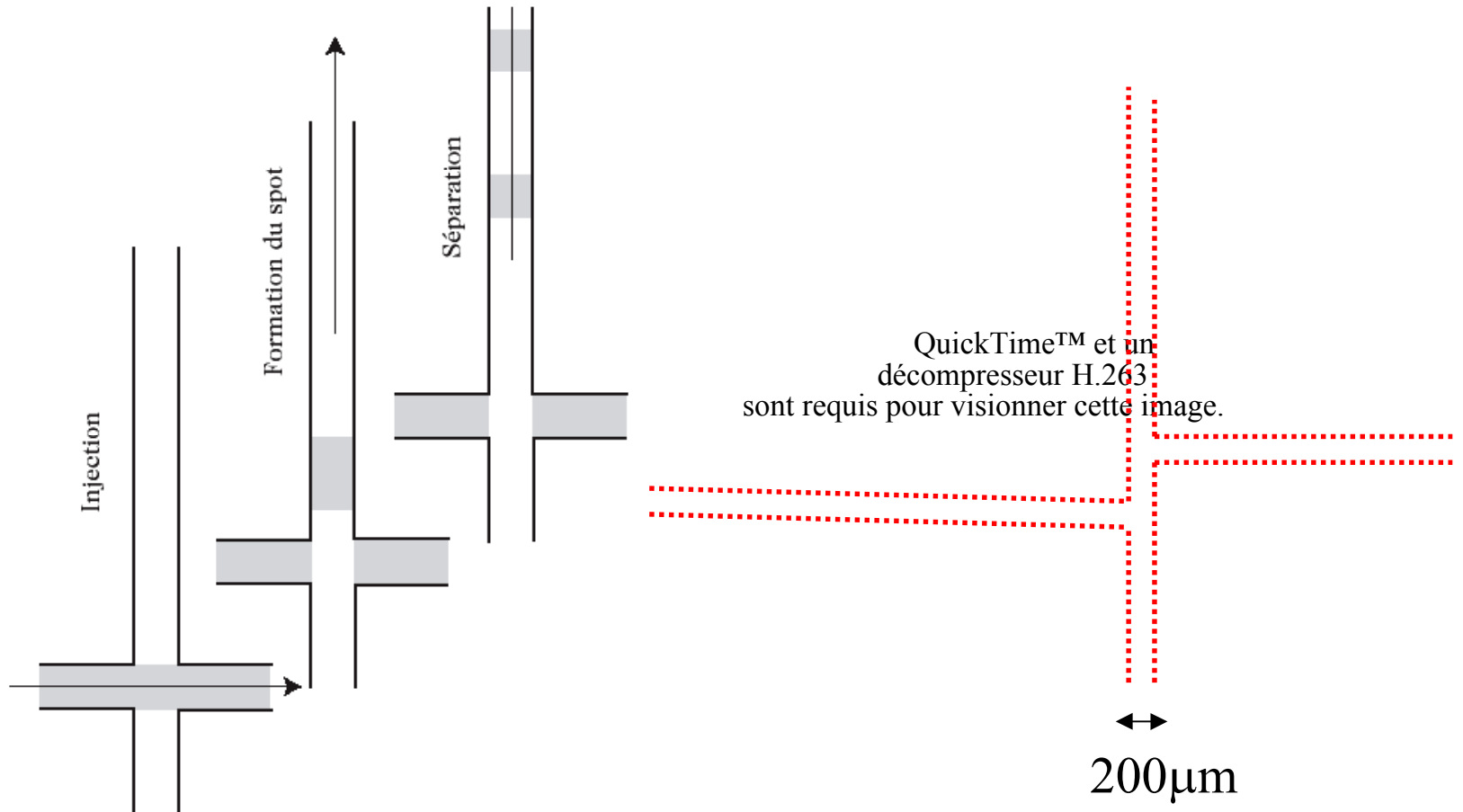
# Miniaturization of electrophoretic separation systems

Caliper



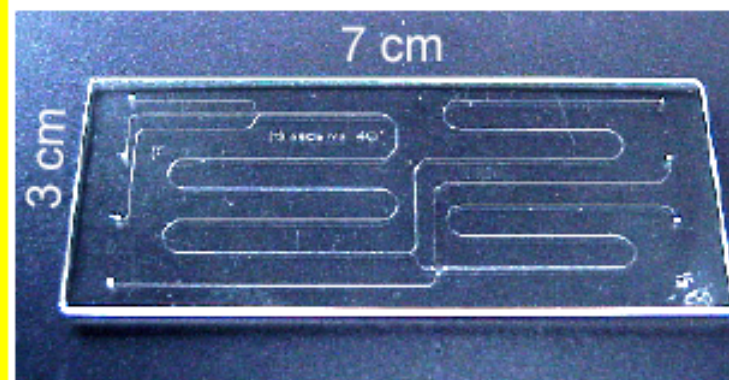
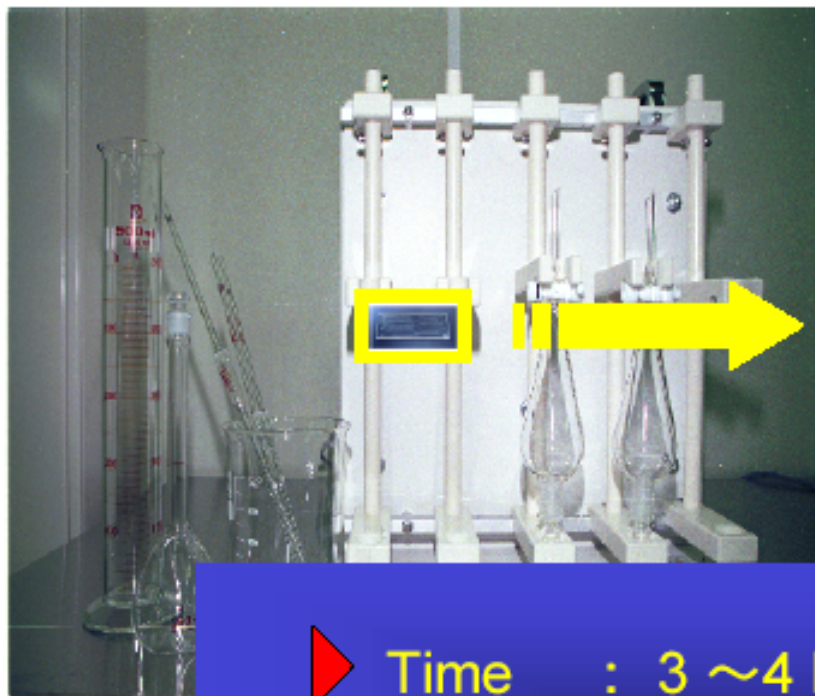
Figure 4.9. Puce commercialisée par la société Caliper permettant une séparation par électrophorèse. Les microcanaux ont été remplis d'un liquide coloré permettant de les visualiser.

# Miniaturization of electrophoretic separation systems



Experiment done by E. Brunet (MMN)

# $\mu$ -Wet Analysis System Environmental Heavy Metal (Co) Analysis Chip

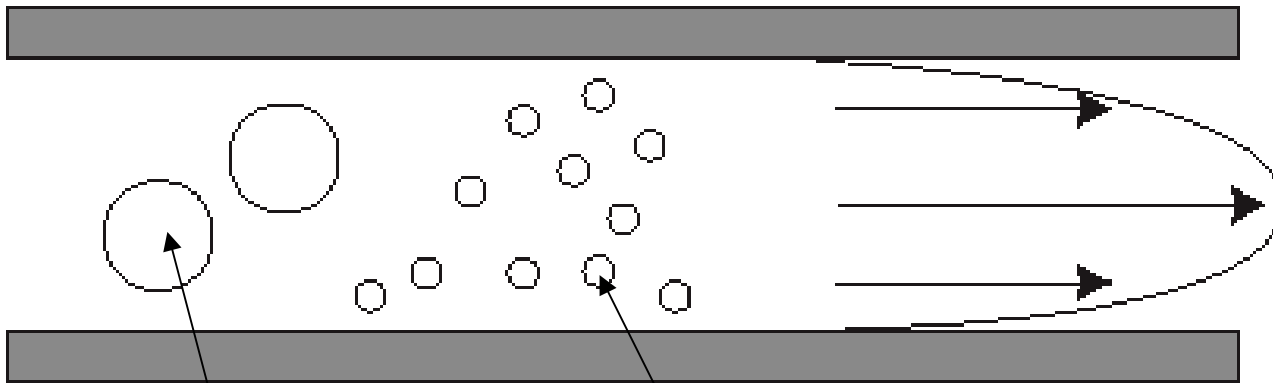


- ▶ Time : 3 ~ 4 hours → 50 sec
- ▶ Quantity : 1 kg → 1  $\mu$ g
- ▶ Sens. : pmol → 0.08 zmol

(From Kitamuri (2004))

SOME DEVELOPMENTS  
OF MICROFLUIDIC SYSTEMS DEDICATED  
TO SEPARATION

# A novel method, based on microfluidics

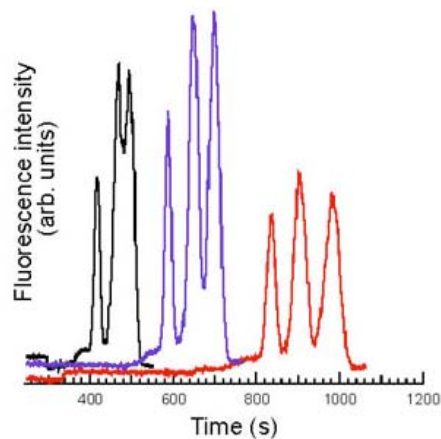
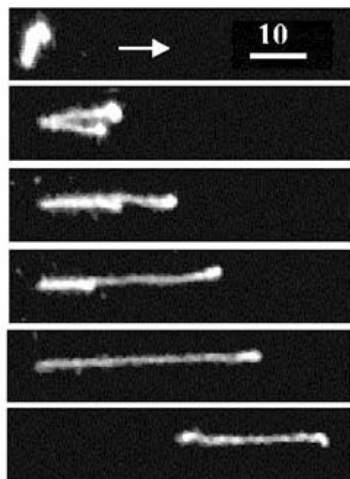
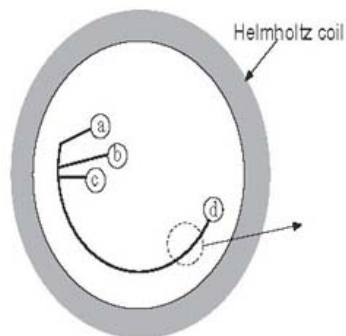
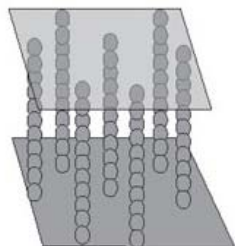


**Big particles  
Move fast**

**Small particles  
move slower**

# Self-Assembled Magnetic Matrices for DNA Separation Chips

Patrick S. Doyle,<sup>1</sup> Jérôme Bibette,<sup>2</sup> Aurélien Bancaud,<sup>3</sup>  
Jean-Louis Viovy<sup>3\*</sup>

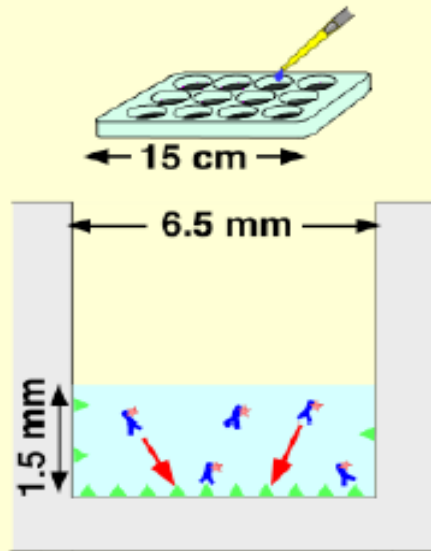


*Institut Curie  
ESPCI*

SAMPLE ANALYSIS IS AN IMPORTANT  
TOPICS IN MICROFLUIDICS.  
ALL SORTS OF SYSTEMS HAVE BEEN  
MICROFABRICATED

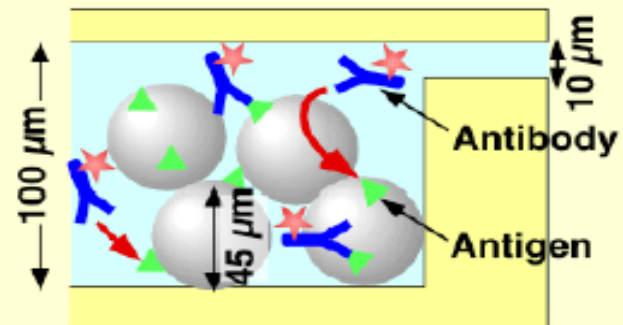
# Macro- & Microspace for Immunoassay

**Microtiter plate  
(Macrospace)**



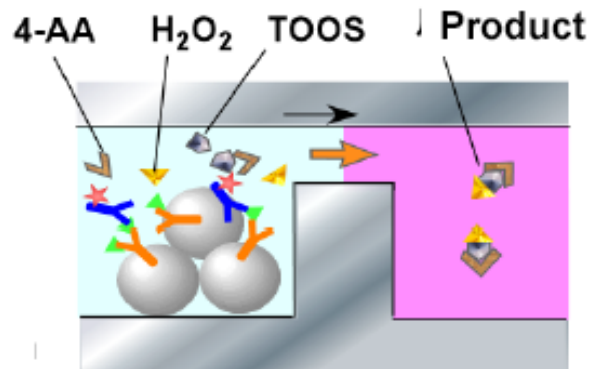
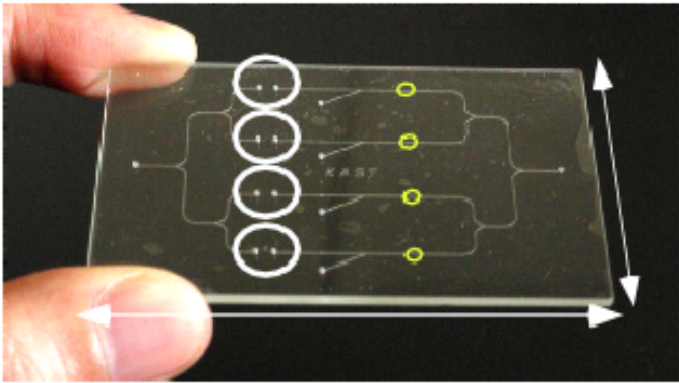
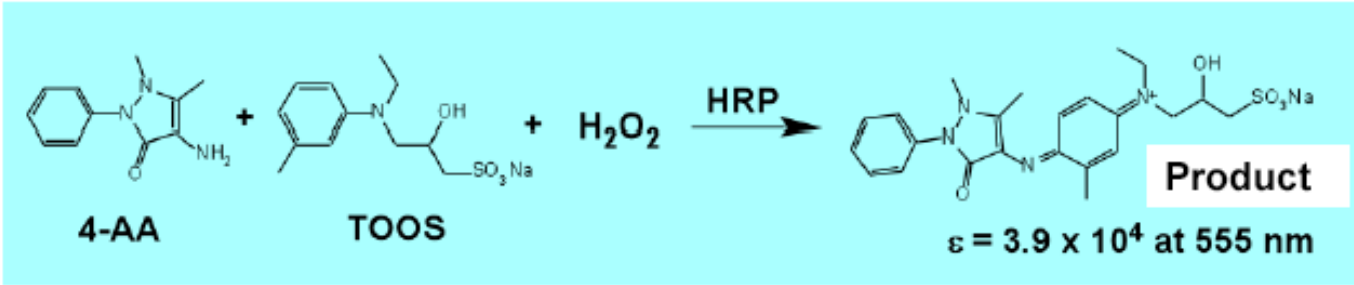
**Diffusion distance  $\sim 1$  mm  
(Reaction time  $\sim 15$  hour)**

**Microchip  
(Microspace)**



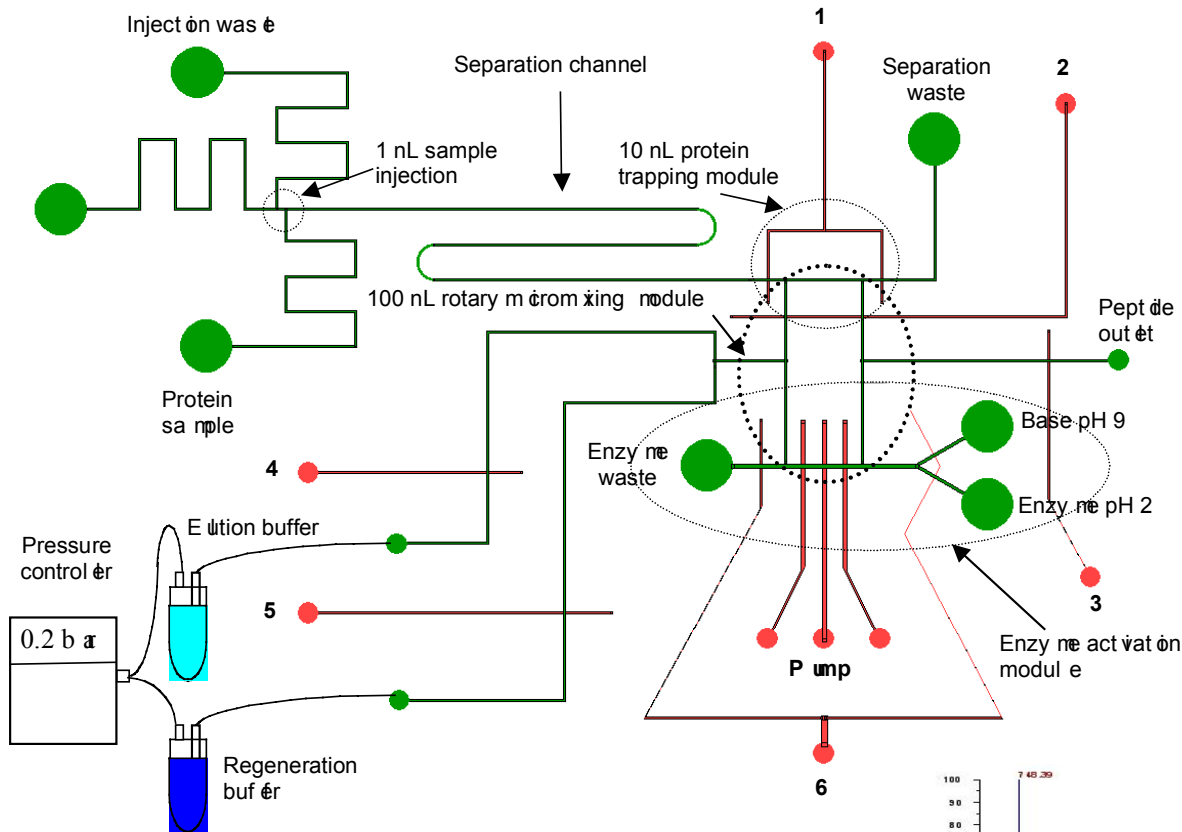
**Diffusion distance  $\sim 10$   $\mu\text{m}$   
(Reaction time  $\sim 10$  min)**

# Multi-Channel Micro ELISA System

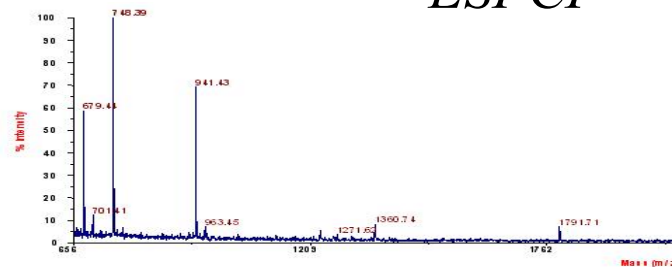


- TLM detection conditions
- Excitation : YAG laser (532 nm)
- Probe : He-Ne (633 nm)

# LAB ON A CHIP DEDICATED TO PROTEOMICS



*Chip demonstrated with a Sample of FITC, Lysozyme, BSA*



*ESPCI*

THIS WAS THE LAST TRANSPARENCY

THANK YOU FOR YOUR KIND ATTENTION

The end